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Real-time Foreground-Background Segmentation Using Codebook Model

K. Kim, T. H. Chalidabhongse, D. Harwood,
and L. Davis

Real-Time Imaging, 2005

Speaker: Shih-Shinh Huang

July 16, 2019





Outline

- Introduction
- Codebook Definition
- Codebook Construction
- Subtraction Process

Introduction

- About Background Subtraction
 - **Assumption:** camera is stationary
 - **Objective:** segment the region of interests (foreground) from the background scenes

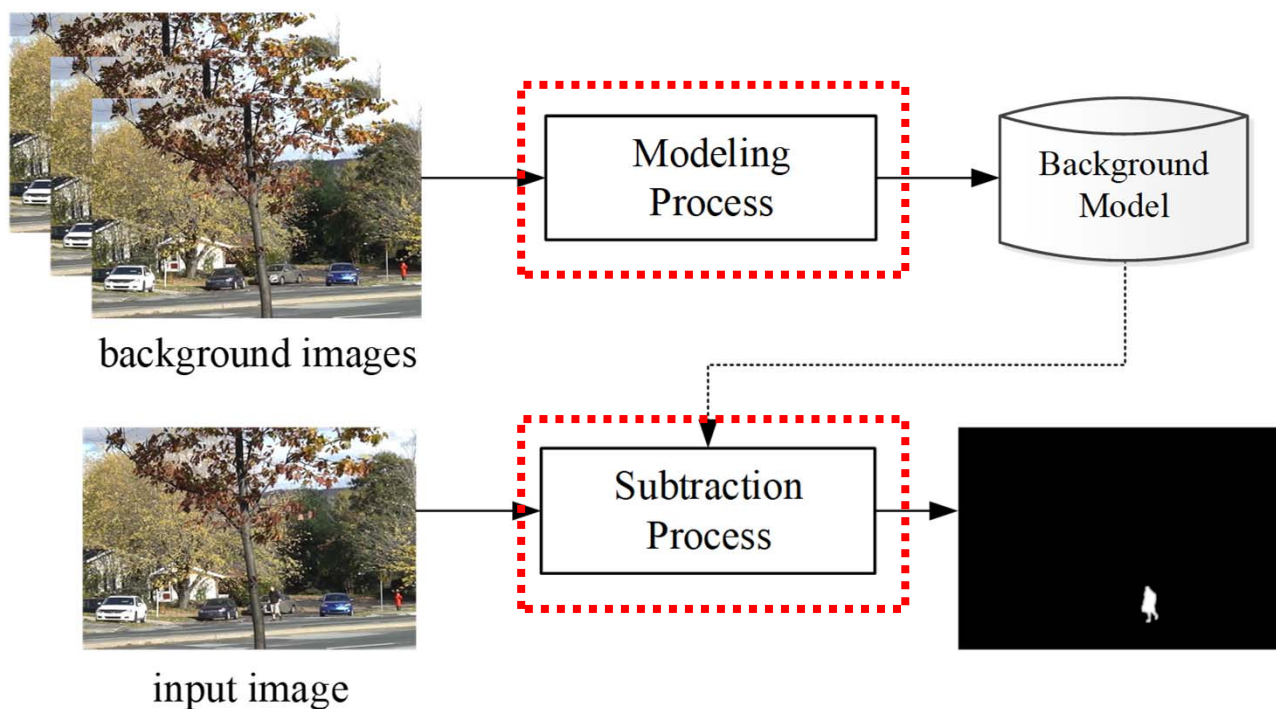
original
image



foreground
mask



Introduction



Subtraction Process: subtract the background from the currently observed image.

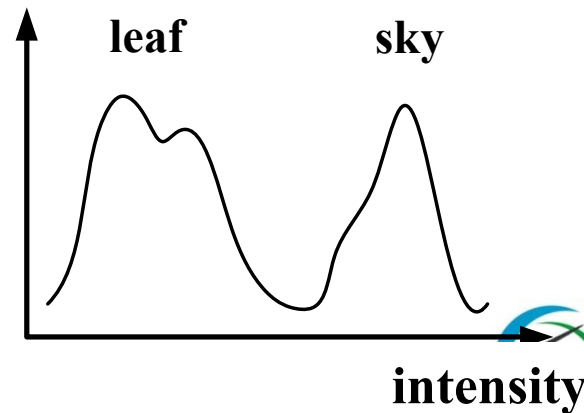
Introduction

- About Background Subtraction
 - The major challenge in background subtraction is dynamic background.
 - contains non-stationary background objects
 - makes it unfeasible to model intensity of a point by a unimodal distribution.



waving tree

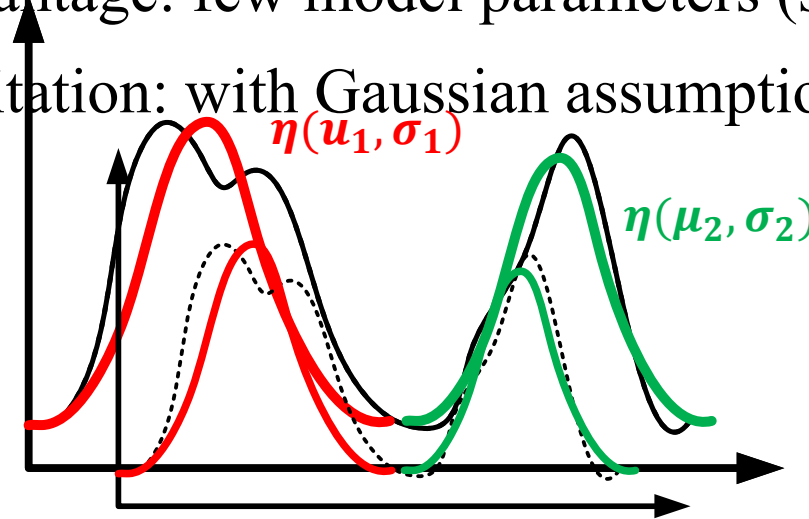
leaf
sky





Introduction

- Dynamic Background Handling
 - Gaussian Mixture Models (GMMs): approximate actual distribution by several Gaussians
 - Advantage: few model parameters (small memory)
 - Limitation: with Gaussian assumption



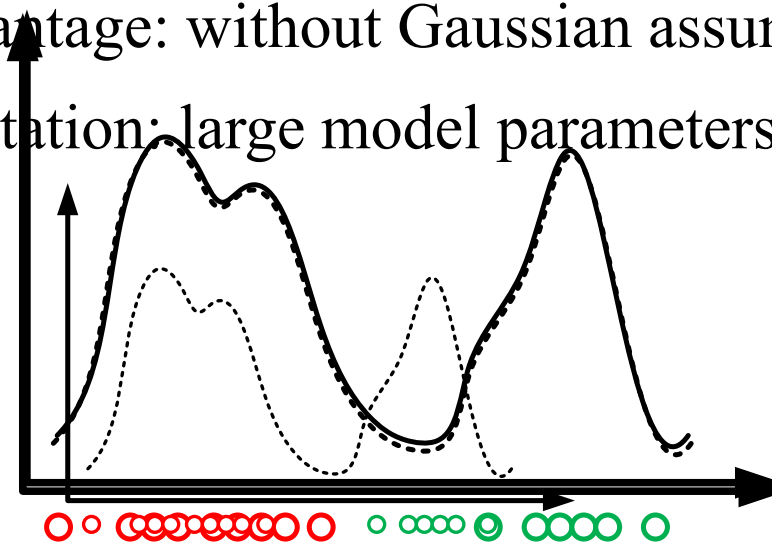
C. Stauffer and W. Grimson, “Adaptive Background Mixture Models for Real Time Tracking”, *CVPR*, 1999.





Introduction

- Dynamic Background Handling
 - **Non-Parametric Model:** approximate actual distribution by a period of samples
 - Advantage: without Gaussian assumption
 - Limitation: large model parameters (large memory)

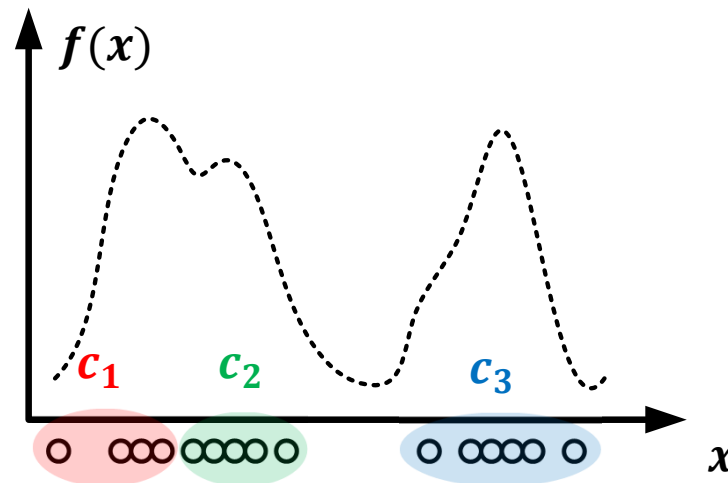


A. Elgammal, D. Harwood, and L. Davis, “Non-Parametric Model for Background Subtraction”, *ECCV*, 2000.



Introduction

- Idea
 - similar to non-parametric model: approximate distributions by a sample set.
 - similar to GMM: describe the sample set by a compact form (called codebook)



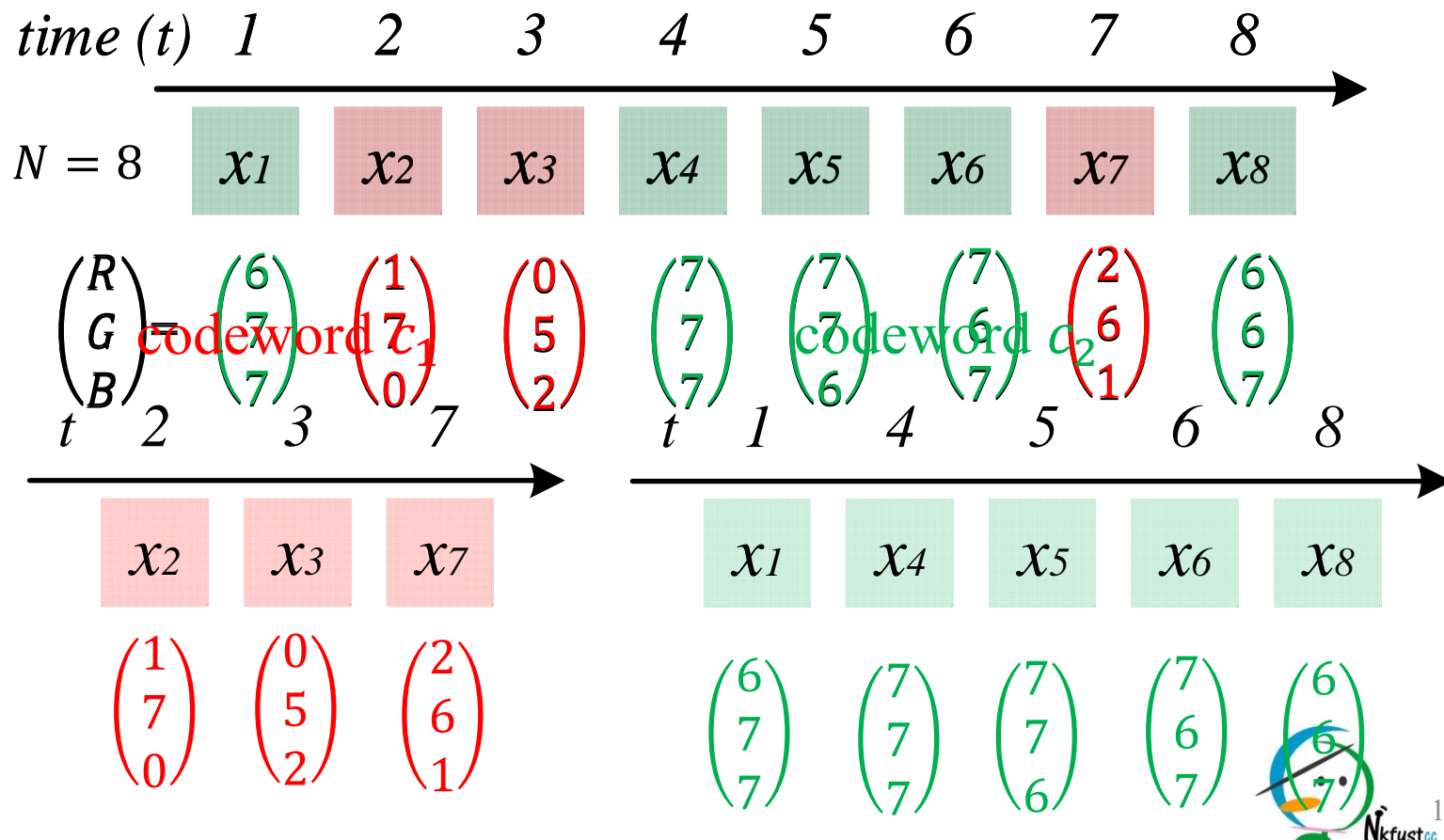


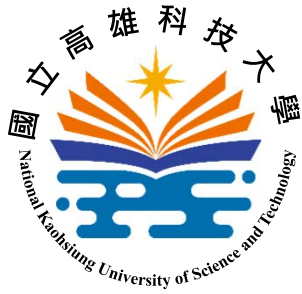
Codebook Definition

- About Codebook B
 - Let $\{x_1, x_2, \dots, x_N\}$ be a sequence of N **background RGB-vectors** of a single point
 - A codebook B is used to describe $\{x_1, x_2, \dots, x_N\}$ by L codewords $\{c_1, c_2, \dots, c_L\}$.
 - Each codeword stands for part of **background RGB-vectors**.

Codebook Definition

- About Codebook B





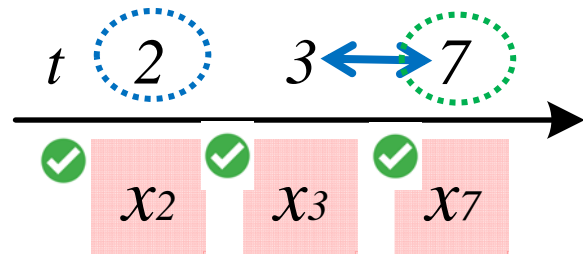
Codebook Definition

- About Codeword c_i
 - A codeword c_i models the sequence of RGB vectors in i th cluster
 - intensity property
 - temporal property
 - Codeword Definition: $c_i = (\mathbf{v}_i, \mathbf{aux}_i)$
 - $\mathbf{v}_i = (\bar{R}_i, \bar{G}_i, \bar{B}_i)$: mean RGB vector
 - $\mathbf{aux}_i = \langle \check{I}_i, \hat{I}_i, f_i, \lambda_i, p_i, q_i \rangle$
 - min/max brightness
 - frequency
 - length (MNRL)
 - negative first/last access time



Codebook Definition

- About Codeword $c_i = (\mathbf{v}_i, \mathbf{aux}_i)$



$$\mathbf{v}_i \equiv \frac{1}{3} \left(\begin{pmatrix} 1 \\ 7 \\ 0 \end{pmatrix}^T + \begin{pmatrix} 0 \\ 5 \\ 2 \end{pmatrix}^T + \begin{pmatrix} 2 \\ 6 \\ 1 \end{pmatrix}^T \right) = \begin{pmatrix} 1 \\ 6 \\ 1 \end{pmatrix}^T$$

$$\begin{pmatrix} R \\ G \\ B \end{pmatrix} = \begin{pmatrix} 1 \\ 7 \\ 0 \end{pmatrix} \quad \begin{pmatrix} 0 \\ 5 \\ 2 \end{pmatrix} \quad \begin{pmatrix} 2 \\ 6 \\ 1 \end{pmatrix}$$

$$I = \begin{pmatrix} 7 \\ 5 \\ 6 \end{pmatrix}$$

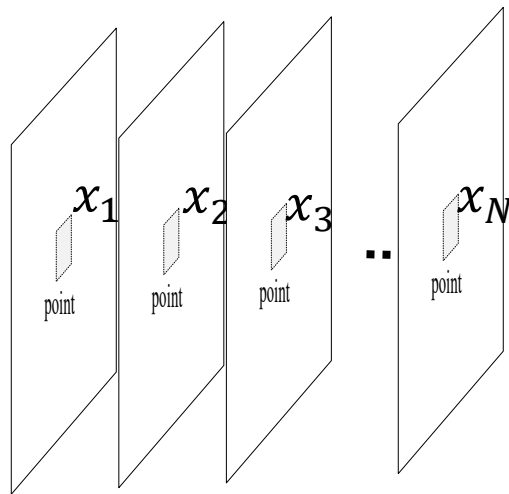
$$\mathbf{aux}_i = \langle \check{I}_i, \hat{I}_i, f_i, \lambda_i, p_i, q_i \rangle$$

- $\check{I}_i = 5, \quad \hat{I}_i = 7$
- $f_i = 3, \quad \lambda_i = 7 - 3 = 4$
- $p_i = 2, \quad q_i = 7$

Codebook Construction

- Formulation

- **Input:** $\{x_1, x_2, \dots, x_N\}$: a sequence of N **training RGB-vectors** of a point
- **Output:** $B = \{c_1, c_2, \dots, c_L\}$



may contain foreground objects

incremental
clustering
→
+ background
codeword selection

$$c_1 = (\mathbf{v}_1, \mathbf{aux}_1)$$

$$c_2 = (\mathbf{v}_2, \mathbf{aux}_2)$$

$$c_3 = (\mathbf{v}_3, \mathbf{aux}_3)$$

⋮

$$c_L = (\mathbf{v}_L, \mathbf{aux}_L)$$



Codebook Construction

- Incremental Clustering
 - Initialization: $B \leftarrow \emptyset$ (empty set)
 - Iterative Step ($t = 1, 2, \dots, N$): sequentially match observation x_t to all codewords $c_i \in B$
 - Case 1 (no match): create a new codeword
 - Case 2 (match found): update the first matched codeword c_m and move it to the first codeword in B



Codebook Construction

- Case 1 (no match)
 - create a new codeword $c = (\mathbf{v}, \mathbf{aux})$ using x_t
 - $\mathbf{v} \leftarrow x_t = (R_t, G_t, B_t)$
 - $\mathbf{aux} \leftarrow \langle I_t, I_t, 1, t - 1, t, t \rangle$



$$\begin{pmatrix} R_2 \\ G_2 \\ B_2 \end{pmatrix} = \begin{pmatrix} 1 \\ 7 \\ 0 \end{pmatrix}$$

$$I_2 = 7$$

$$\mathbf{v} = \langle 1, 7, 0 \rangle$$

$$\mathbf{aux} = \langle \check{I}, \hat{I}, f, \lambda, p, q \rangle$$

- $\check{I} = \hat{I} = 7$
- $f = 1, \quad \lambda = 2 - 1 = 1$
- $p = 2, \quad q = 2$

Codebook Construction

- Case 2 (match found)
 - update first matched $c_m = (\mathbf{v}_m, \mathbf{aux}_m)$

$$\mathbf{v}_m = (\bar{R}_m, \bar{G}_m, \bar{B}_m) \quad \mathbf{aux}_m = \langle \check{I}_m, \hat{I}_m, f_m, \lambda_m, p_m, q_m \rangle$$

$$\Downarrow x_t = (R_t, G_t, B_t)$$

$$\mathbf{v}_m = \left(\frac{f_m \times \bar{R}_m + R_t}{f_m + 1}, \frac{f_m \times \bar{G}_m + G_t}{f_m + 1}, \frac{f_m \times \bar{B}_m + B_t}{f_m + 1} \right)$$

$$\mathbf{aux}_m = \langle \min(\check{I}_m, I_t), \max(\hat{I}_m, I_t), f_m + 1, \max(\lambda_m, t - q_m), p_m, t \rangle$$



Codebook Construction

- Case 2 (match found)



$$\begin{pmatrix} R_3 \\ G_3 \\ B_3 \end{pmatrix} = \begin{pmatrix} 0 \\ 5 \\ 2 \end{pmatrix}$$

$$I_3 = 5$$

$$\mathbf{v}_m = \langle 1, 7, 0 \rangle$$

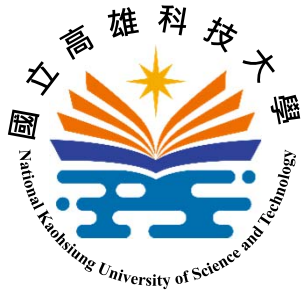
$$\mathbf{aux}_m = \langle \check{I}_m = 7, \hat{I}_m = 7, f_m = 1, \lambda_m = 1, p_m = 2, q_m = 2 \rangle$$

↓ $x_3 = (0, 5, 2)$

$$\mathbf{v}_m = \langle \frac{1 \times 1 + 0}{1 + 1}, \frac{1 \times 7 + 5}{1 + 1}, \frac{1 \times 0 + 2}{1 + 1} \rangle$$

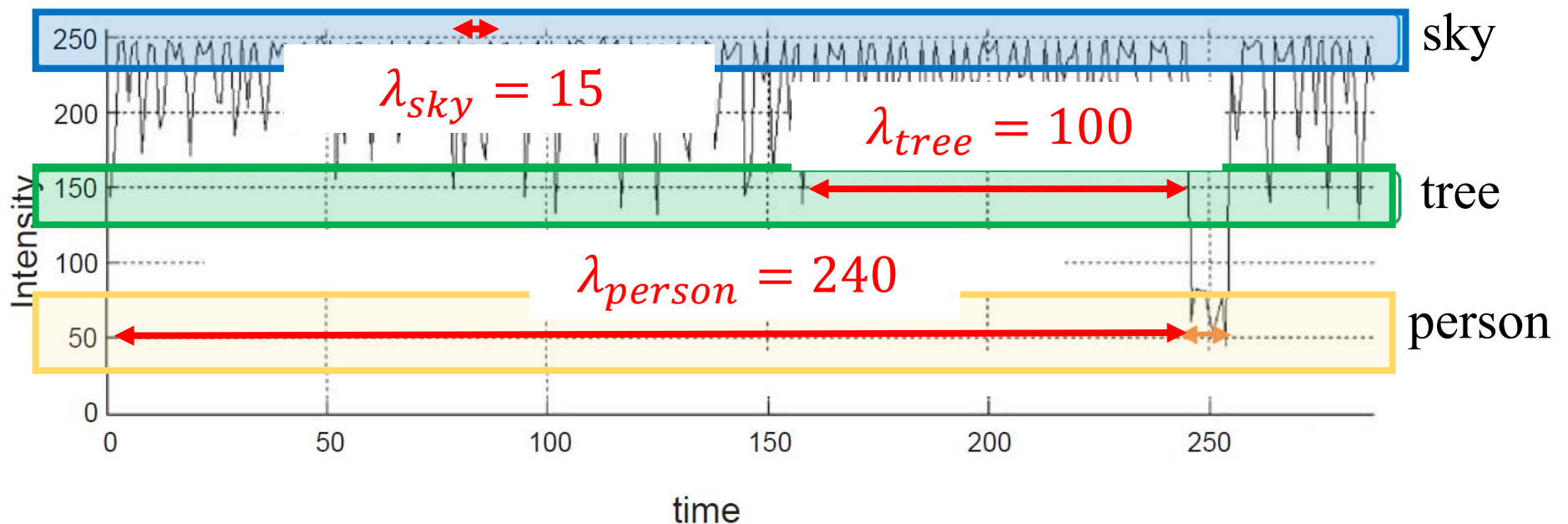
$$\mathbf{aux}_m = \langle \check{I}_m = \min(7, 5), \hat{I}_m = \max(7, 5), 2, + 1, \lambda_m = \max(1, 2), p_m = 2, q_m = 2 \rangle$$

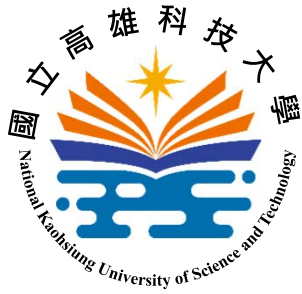
$$\lambda_m = \max(1, 2), p_m = 2, q_m = 2$$



Codebook Construction

- Background Codeword Selection
 - **Objective:** select codewords representing the static or dynamic background points.





Codebook Construction

- Background Codeword Selection
 - **Observation:** true background is quasi-periodic, that is, values recur in a bounded period
 - **Rule:** take the codewords with small λ

$$B = \{c_m | \lambda_m \leq T\}$$

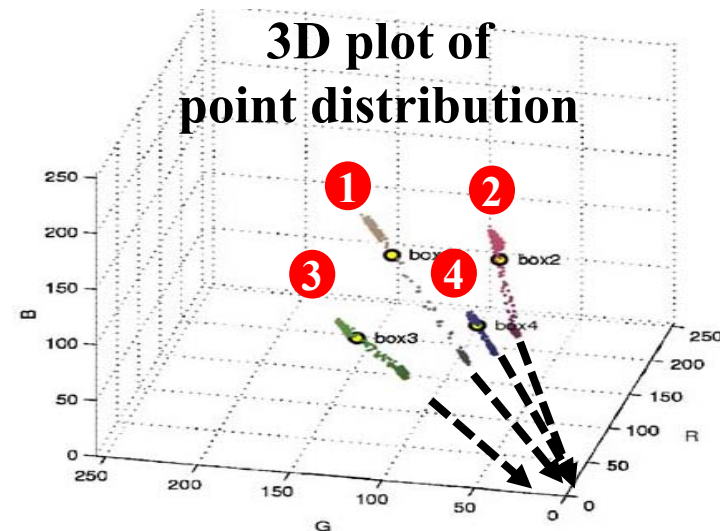
- T : a threshold value (half the number of training frames $N/2$)

Subtraction Process

- Color Model of a Codeword
 - The shape of point intensity distribution has two attributes.
 - elongated
 - toward the origin (0,0,0)



color chart image

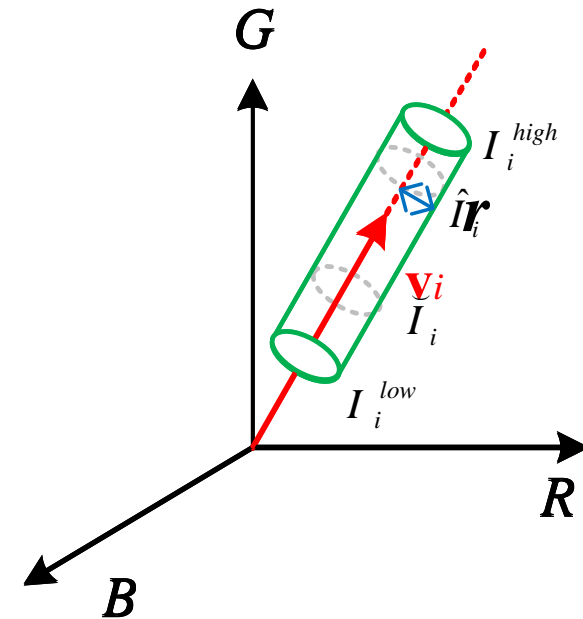


Subtraction Process

- Color Model of a Codeword
 - The color model defined by $c_i = (\mathbf{v}_i, \mathbf{aux}_i)$ is a cylinder.
 - \mathbf{v}_i : major axis of cylinder
 - γ : cylinder radius (constant)
 - $[I_i^{low}, I_i^{high}]$: top/bottom bases

$$I_i^{low} = \alpha \hat{I}_i \quad [0.4, 0.7]$$

$$I_i^{high} = \min(\beta \hat{I}_i, \frac{\check{I}_i}{\alpha}) \quad [1.1, 1.5]$$





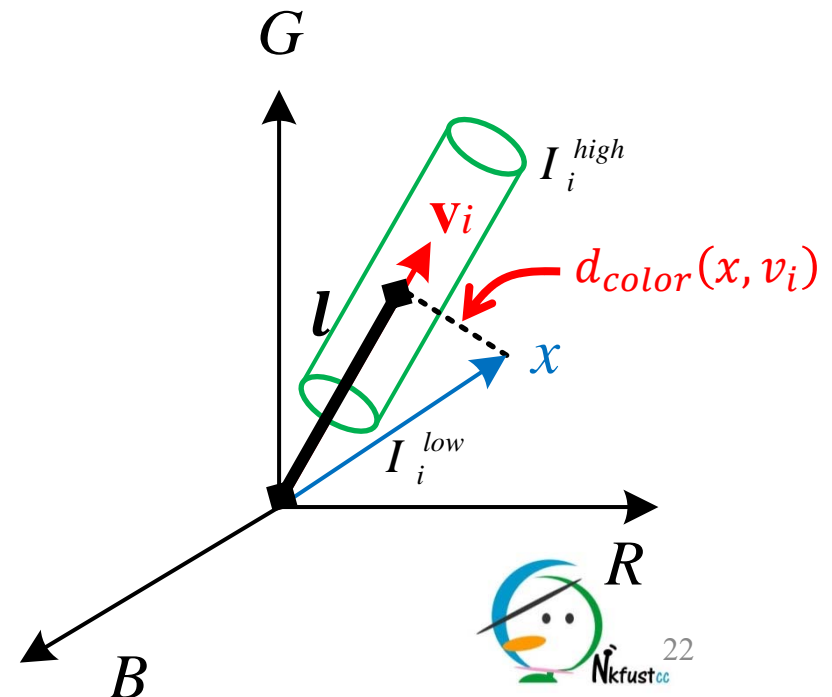
Subtraction Process

- Match Definition $M(x, c_i)$
 - $M(x, c_i)=1$: x is in the c_i -defined cylinder.

- $d_{color}(x, v_i) \leq \gamma$ and

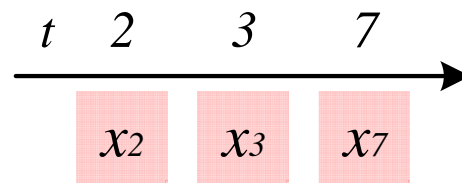
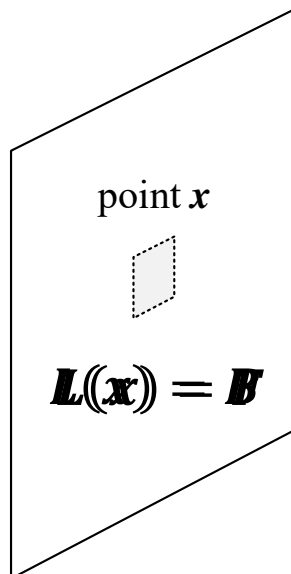
- $I_i^{low} \leq ||x|| \leq I_i^{high}$

$$d_{color}(x, v_i) = \sqrt{||x||^2 - l^2}$$
$$l^2 = \frac{\langle x, v_i \rangle^2}{||v_i||^2}$$



Subtraction Process

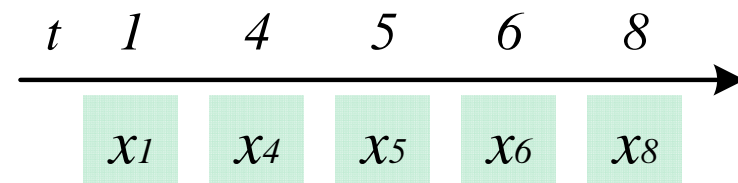
- Point Labelling ($L(x)$)
 - $L(x) = B$: at least one codeword is matched.
 - $L(x) = F$: none of codewords are matched



$$c_1 = (v_1, \mathbf{aux}_1)$$

$$\times M(x, c_1) \equiv 0_1$$

mis-matched



$$c_2 = (v_2, \mathbf{aux}_2)$$

$$\times M(x, c_2) \equiv 0$$

mis-matched

